

In Exercises 3–24, find the derivative of the function.

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|-----------------------------|------------------------------|
| 3. $y = 8$                  | 4. $f(x) = -2$               |
| 5. $y = x^6$                | 6. $y = x^8$                 |
| 7. $y = \frac{1}{x^7}$      | 8. $y = \frac{1}{x^8}$       |
| 9. $f(x) = \sqrt[3]{x}$     | 10. $g(x) = \sqrt[4]{x}$     |
| 11. $f(x) = x + 1$          | 12. $g(x) = 3x - 1$          |
| 13. $f(t) = -2t^2 + 3t - 6$ | 14. $y = t^2 + 2t - 3$       |
| 15. $g(x) = x^2 + 4x^3$     | 16. $y = 8 - x^3$            |
| 17. $s(t) = t^3 - 2t + 4$   | 18. $f(x) = 2x^3 - x^2 + 3x$ |

In Exercises 31–38, find the slope of the graph of the function at the indicated point. Use the derivative feature of a graphing utility to confirm your results.

Function	Point
31. $f(x) = \frac{3}{x^2}$	(1, 3)
32. $f(t) = 3 - \frac{3}{5t}$	( $\frac{3}{5}$ , 2)
33. $f(x) = -\frac{1}{2} + \frac{7}{5}x^3$	(0, $-\frac{1}{2}$ )
34. $y = 3x^3 - 6$	(2, 18)
35. $y = (2x + 1)^2$	(0, 1)
36. $f(x) = 3(5 - x)^2$	(5, 0)
37. $f(\theta) = 4 \sin \theta - \theta$	(0, 0)
38. $g(t) = 2 + 3 \cos t$	( $\pi$ , -1)

In Exercises 39–52, find the derivative of the function.

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|---|---|
| 39. $f(x) = x^2 + 5 - 3x^{-2}$          | 40. $f(x) = x^2 - 3x - 3x^{-2}$               |
| 41. $g(t) = t^2 - \frac{4}{t^3}$        | 42. $f(x) = x + \frac{1}{x^2}$                |
| 43. $f(x) = \frac{x^3 - 3x^2 + 4}{x^2}$ | 44. $h(x) = \frac{2x^2 - 3x + 1}{x}$          |
| 45. $y = x(x^2 + 1)$                    | 46. $y = 3x(6x - 5x^2)$                       |
| 47. $f(x) = \sqrt{x} - 6\sqrt[3]{x}$    | 48. $f(x) = \sqrt[3]{x} + \sqrt[5]{x}$        |
| 49. $h(s) = s^{4/5} - s^{2/3}$          | 50. $f(t) = t^{2/3} - t^{1/3} + 4$            |
| 51. $f(x) = 6\sqrt{x} + 5 \cos x$       | 52. $f(x) = \frac{2}{\sqrt[3]{x}} + 3 \cos x$ |

In Exercises 53–56, (a) find an equation of the tangent line to the graph of  $f$  at the indicated point, (b) use a graphing utility to graph the function and its tangent line at the point, and (c) use the derivative feature of a graphing utility to confirm your results.

Function	Point
53. $y = x^4 - 3x^2 + 2$	(1, 0)
54. $y = x^3 + x$	(-1, -2)
55. $f(x) = \frac{2}{\sqrt[4]{x^3}}$	(1, 2)
56. $y = (x^2 + 2x)(x + 1)$	(1, 6)

In Exercises 57–62, determine the point(s) (if any) at which the graph of the function has a horizontal tangent line.

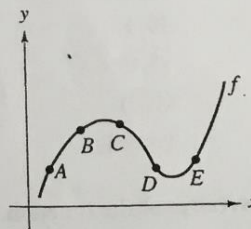
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|---|-------------------|
| 57. $y = x^4 - 8x^2 + 2$                              | 58. $y = x^3 + x$ |
| 59. $y = \frac{1}{x^2}$                               | 60. $y = x^2 + 1$ |
| 61. $y = x + \sin x, \quad 0 \leq x < 2\pi$           |                   |
| 62. $y = \sqrt{3}x + 2 \cos x, \quad 0 \leq x < 2\pi$ |                   |

In Exercises 63–66, find  $k$  such that the line is tangent to the graph of the function.

Function	Line
63. $f(x) = x^2 - kx$	$y = 4x - 9$
64. $f(x) = k - x^2$	$y = -4x + 7$
65. $f(x) = \frac{k}{x}$	$y = -\frac{3}{4}x + 3$
66. $f(x) = k\sqrt{x}$	$y = x + 4$

### Getting at the Concept

67. Use the graph of  $f$  to answer each question. To print an enlarged copy of the graph, go to the website [www.mathgraphs.com](http://www.mathgraphs.com).



- Between which two consecutive points is the average rate of change of the function greatest?
  - Is the average rate of change of the function between A and B greater than or less than the instantaneous rate of change at B?
  - Sketch a tangent line to the graph between C and D such that the slope of the tangent line is the same as the average rate of change of the function between C and D.
68. Sketch the graph of a function  $f$  such that  $f' > 0$  for all  $x$  and the rate of change of the function is decreasing.