

1.

Let  $g(x) = \frac{x}{\sqrt{2-x^2}}$

[3 points]

a) Find  $g'(x)$  and simplify it to match one of the following choices (show all of your work!):

(i)  $g'(x) = \frac{2}{(2-x^2)^{3/2}}$

(ii)  $g'(x) = \frac{-1}{2(2-x^2)^{3/2}}$

(iii)  $g'(x) = \frac{-x^2 - \frac{1}{2}x + 2}{(2-x^2)^{3/2}}$

b) For what value(s) of  $x$  is the tangent line to the curve  $g(x)$  horizontal?

$$g' = \frac{\sqrt{2-x^2}(1) - \frac{1}{2}(2-x^2)^{-1/2}(-2x)(x)}{2-x^2}$$

$$g' = \frac{(2-x^2)^{1/2} + \frac{x^2}{(2-x^2)^{1/2}}}{2-x^2}$$

$$g' = \frac{2}{(2-x^2)^{3/2}}$$

Get CD

$$\frac{2}{(2-x^2)^{3/2}} = \frac{1}{(2-x^2)}$$

$$\frac{2-x^2+x^2}{(2-x^2)^{1/2}}$$

2.  $f(x) = f(x) = \begin{cases} cx + d, & x \leq 2 \\ x^2 - cx, & x > 2 \end{cases}$  where  $c$  and  $d$  are constants.

If  $f$  is differentiable at  $x=2$ . What is the value of  $c + d$

$$\lim_{x \rightarrow 2^-} f'(x) = c = \lim_{x \rightarrow 2^+} f'(x) = 2x - c$$

$$\frac{c}{c} = \frac{2x - c}{c}$$

$$2c = 2(2) - c$$

$$c = 2$$

$$\lim_{x \rightarrow 2} f(x) = 2(2) + d = 4 + d$$

$$4 + d = 0$$

$$d = -4$$

$$c + d = 2 + (-4) = -2$$

3. Find  $\frac{dy}{dx}$  for the curve  $y = \frac{2^{\sin x}}{\cos x}$

$$y = 2^{\sin x}$$

$$du = \cos x$$

$$\frac{2^y \ln 2}{\cos x}$$

a)  $-2^{\sin x} \ln 2 \cot x$

b)  $2^{\sin x} \ln 2 \cos x \sec x \tan x$

c)  $-2^{\sin x} \ln 2 \tan x$

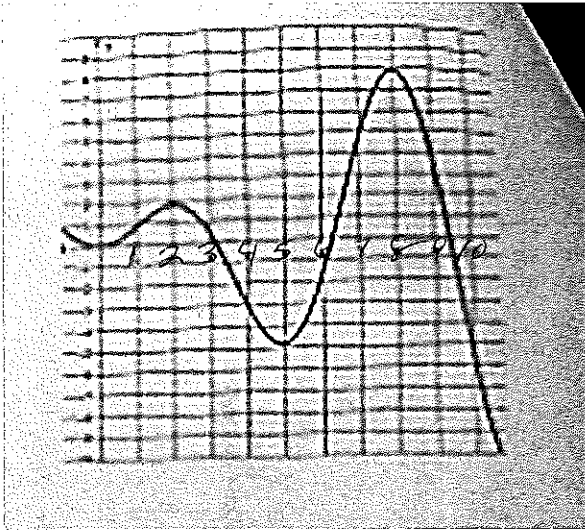
d)  $2^{\sin x} \left( \ln 2 + \frac{\sin x}{\cos^2 x} \right)$

e)  $2^{\sin x} (\ln 2 + \tan^2 x)$

$$\frac{(\cos x) 2^{\sin x} \ln 2 \cos x - (2^{\sin x}) 2^{\sin x}}{(\cos x)^2}$$

$$2^{\sin x} \frac{(\cos x)^2 \ln 2 + \sin x}{(\cos x)^2}$$

4. The graph shown below represents the velocity function for a particle. At what approximate times is the particle speeding up? Use interval notation



speeding up

$$(0, 2) \quad (3, 5) \quad (6.5, 8) \quad (9.5, 10)$$

5. use calculator

Two particles move along the x-axis, and their positions for  $0 \leq t \leq 2\pi$  are given by

$x_1 = \cos(2t)$  and  $x_2(t) = e^{\frac{t-3}{2}} - .75$  for what values of  $t$  in that interval do the particles have the same velocity?

$$v_1(t) = -2\sin(2t) = v_2(t) = e^{\frac{t-3}{2}}$$

$$u = \frac{1}{2}t^{-3/2}$$

$$du = -\frac{3}{4}t^{-5/2}$$

$$\boxed{\begin{matrix} (1.634, -2.52) & (5.113, 1.438) \\ (3.014, .503) & (5.662, 1.892) \end{matrix}}$$

6. for the curve  $x^2 + y^4 = 10$

a. Find the points at which the curve has a horizontal tangent(s)

b. find the equation of the tangent line at the point where  $y=1$

c. find  $\frac{d^2y}{dx^2}$ , be sure there are no  $\frac{dy}{dx}$ 's in your answer, and simplify completely.

$$2x + 4y^3 y' = 0$$

$$\frac{4y^3 y'}{4y^3} = \frac{-2x}{4y^3}$$

$$y' = \frac{-x}{2y^3}$$

$$\textcircled{b} \quad \begin{matrix} x^2 + y^4 = 10 \\ x^2 + 1 = 10 \\ x^2 = 9 \\ x = \pm 3 \end{matrix}$$

$$y' = \frac{-3}{2(1)} = -\frac{3}{2}$$

$$y' = \frac{+3}{2} = \frac{+3}{2}$$

$$\textcircled{c} \quad \frac{(2y^3)(-1) - 6y^2 y'(-x)}{(2y^3)^2}$$

sub in  $\downarrow$

$$\frac{-2y^3 + 6xy^2 \left(\frac{-x}{2y^3}\right)}{(2y^3)^2}$$

then simplify

$$\boxed{y'' = \frac{-1}{2y^3} - \frac{3x^2}{4y^7}}$$

$\textcircled{a}$

$$\begin{matrix} x = 0 \\ y = \sqrt[4]{10} \end{matrix}$$

$$\text{at } (3, 1) \quad y - 1 = -\frac{3}{2}(x - 3) \quad \text{at } (-3, 1) \quad y - 1 = \frac{+3}{2}(x + 3)$$