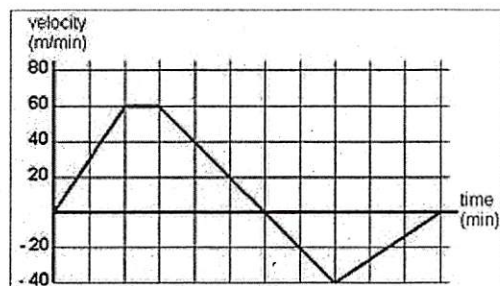


To be successful you must accept all challenges that come your way. You can't just accept the ones you like. ~Mike Gafka

Velocity for chapter 6

AP Calculus AB



1. The velocity of a particle is given on the right. The position of the particle at $t=0$ is 3.

- What is the total distance traveled from $t=0$ to $t=6$?

$$\int_0^6 |v(t)| dt = 210$$

- What is the total distance traveled from $t=0$ to $t=8$?

$$\int_0^8 |v(t)| dt = 250$$

- What is the total distance traveled from $t=0$ to $t=11$?

$$\int_0^{11} |v(t)| dt = 310$$

- What is the displacement of the particle from $t=0$ to $t=6$?

$$\int_0^6 v(t) dt = 210$$

- What is the displacement of the particle from $t=0$ to $t=8$?

$$\int_0^8 v(t) dt = 170$$

- What is the displacement of the particle from $t=0$ to $t=11$?

$$\int_0^{11} v(t) dt = 110$$

- Where is the particle at $t=6$? At $t=11$?

$$3 + \int_0^6 v(t) dt = 213 \text{ m} \quad 3 + \int_0^{11} v(t) dt = 113$$

2. Given $v(t) = 4 - t^2$ and $s(0) = -4$ units

- Find the total distance the particle traveled from $t=0$ to 3 seconds.

$$\int_0^2 v(t) dt + \int_2^3 |v(t)| dt = 23/3$$

$$4t - \frac{t^3}{3} \Big|_0^2 \quad 8 - \frac{8}{3} - (0)$$

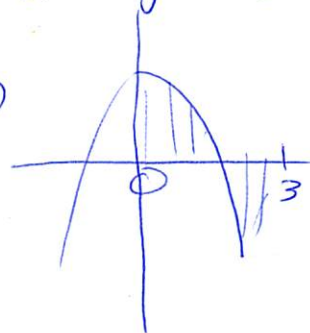
- Find the displacement of the particle from $t=0$ to 3 seconds.

$$\int_0^3 4 - t^2 dt = 3$$

- Where is the particle at $t=3$ sec?

$$-4 + \int_0^3 v(t) dt = -1$$

(Don't forget to integrate)



No calc

To be successful you must accept all challenges that come your way. You can't just accept the ones you like. ~Mike Gafka

Velocity for chapter 6

AP Calculus AB

NOTES:

Displacement of the particle on $[a,b] = \int_a^b v(t) dt$

Total distance traveled of the particle on $[a,b] = \int_a^b |v(t)| dt$

Position of the particle at $t = a$: initial position + displacement = $s(0) + \int_0^a v(t) dt$

If given a position other than at $t = 0$ just set up a definite integral of $v(t)$ with the position you are given and the one you are looking for and use FTC and algebra to solve for the position you are looking for.

Ex. If given $s(3) = 8$ and you want to find $s(10)$:

$$\int_3^{10} v(t) dt = s(10) - s(3) \quad \text{so then} \quad s(10) = s(3) + \int_3^{10} v(t) dt = 8 + \int_3^{10} v(t) dt$$

If instead you want to find $s(1)$ still knowing that $s(3) = 8$:

$$\int_1^3 v(t) dt = s(3) - s(1) \quad \text{so then} \quad s(1) = s(3) - \int_1^3 v(t) dt = 8 - \int_1^3 v(t) dt$$

Calculator Question:

A particle moves along the x-axis so that at any time $t > 0$ its velocity is given by $v(t) = t \ln t - t$. At time $t = 1$, the position of the particle is $x(1) = 6$.

$v(t) = 0$
 $v'(t) = 1$

- a) When is the particle at rest? 2.718
- b) For what values of t is the particle moving to the right? $(2.718, \infty)$
- c) Find the acceleration of the particle at time $t = 5$. 1.609
- d) When is the particle's acceleration zero? 1
- e) Find the total distance traveled by the particle from $t = 1$ to $t = 8$. $\int_1^8 |v(t)| = 21.864$
- f) Find the displacement of the particle from $t = 1$ to $t = 8$. $\int_1^8 v(t) = 19.292$
- g) Find the position of the particle at $t = 5$. $6 + \int_1^5 v(t) = 8.117$
- h) Find the position of the particle at $t = 0.3$. $6 - \int_{0.3}^1 v(t) = 6 - (-.628) = 6.628$
- i) For what values of t is the particle slowing down? Speeding up?

I slowing down
 $v(t) + a(t)$
different signs
 $(1, \infty)$

I speeding up
 $v(t) + a(t)$
same sign
 $(0, 1) (e, \infty)$

$$A(x) = x \cdot \frac{1}{x} + 1 \ln x - 1$$

$$A(x) = \ln x$$