

2003 AP<sup>®</sup> CALCULUS AB FREE-RESPONSE QUESTIONS (Form B)

2. A tank contains 125 gallons of heating oil at time  $t = 0$ . During the time interval  $0 \leq t \leq 12$  hours, heating oil is pumped into the tank at the rate

$$H(t) = 2 + \frac{10}{(1 + \ln(t + 1))} \text{ gallons per hour.}$$

During the same time interval, heating oil is removed from the tank at the rate

$$R(t) = 12 \sin\left(\frac{t^2}{47}\right) \text{ gallons per hour.}$$

- How many gallons of heating oil are pumped into the tank during the time interval  $0 \leq t \leq 12$  hours?
- Is the level of heating oil in the tank rising or falling at time  $t = 6$  hours? Give a reason for your answer.
- How many gallons of heating oil are in the tank at time  $t = 12$  hours?
- At what time  $t$ , for  $0 \leq t \leq 12$ , is the volume of heating oil in the tank the least? Show the analysis that leads to your conclusion.

AP<sup>®</sup> CALCULUS AB  
2002 SCORING GUIDELINES (Form B)

Question 2

The number of gallons,  $P(t)$ , of a pollutant in a lake changes at the rate  $P'(t) = 1 - 3e^{-0.2\sqrt{t}}$  gallons per day, where  $t$  is measured in days. There are 50 gallons of the pollutant in the lake at time  $t = 0$ . The lake is considered to be safe when it contains 40 gallons or less of pollutant.

- Is the amount of pollutant increasing at time  $t = 9$ ? Why or why not?
- For what value of  $t$  will the number of gallons of pollutant be at its minimum? Justify your answer.
- Is the lake safe when the number of gallons of pollutant is at its minimum? Justify your answer.
- An investigator uses the tangent line approximation to  $P(t)$  at  $t = 0$  as a model for the amount of pollutant in the lake. At what time  $t$  does this model predict that the lake becomes safe?

AP<sup>®</sup> CALCULUS AB  
2004 SCORING GUIDELINES (Form B)

Question 2

3 Calc  
For  $0 \leq t \leq 31$ , the rate of change of the number of mosquitoes on Tropical Island at time  $t$  days is modeled by  $R(t) = 5\sqrt{t} \cos\left(\frac{t}{5}\right)$  mosquitoes per day. There are 1000 mosquitoes on Tropical Island at time  $t = 0$ .

- (a) Show that the number of mosquitoes is increasing at time  $t = 6$ .
- (b) At time  $t = 6$ , is the number of mosquitoes increasing at an increasing rate, or is the number of mosquitoes increasing at a decreasing rate? Give a reason for your answer.
- (c) According to the model, how many mosquitoes will be on the island at time  $t = 31$ ? Round your answer to the nearest whole number.
- (d) To the nearest whole number, what is the maximum number of mosquitoes for  $0 \leq t \leq 31$ ? Show the analysis that leads to your conclusion.

4 Calc  
AP<sup>®</sup> CALCULUS AB  
2010 SCORING GUIDELINES

Question 1

There is no snow on Janet's driveway when snow begins to fall at midnight. From midnight to 9 A.M., snow accumulates on the driveway at a rate modeled by  $f(t) = 7te^{\cos t}$  cubic feet per hour, where  $t$  is measured in hours since midnight. Janet starts removing snow at 6 A.M. ( $t = 6$ ). The rate  $g(t)$ , in cubic feet per hour, at which Janet removes snow from the driveway at time  $t$  hours after midnight is modeled by

$$g(t) = \begin{cases} 0 & \text{for } 0 \leq t < 6 \\ 125 & \text{for } 6 \leq t < 7 \\ 108 & \text{for } 7 \leq t \leq 9. \end{cases}$$

- (a) How many cubic feet of snow have accumulated on the driveway by 6 A.M.?
- (b) Find the rate of change of the volume of snow on the driveway at 8 A.M.
- (c) Let  $h(t)$  represent the total amount of snow, in cubic feet, that Janet has removed from the driveway at time  $t$  hours after midnight. Express  $h$  as a piecewise-defined function with domain  $0 \leq t \leq 9$ .
- (d) How many cubic feet of snow are on the driveway at 9 A.M.?

2004 AP<sup>®</sup> CALCULUS AB FREE-RESPONSE QUESTIONS

CALCULUS AB  
SECTION II, Part A

Time—45 minutes

Number of problems—3

A graphing calculator is required for some problems or parts of problems.

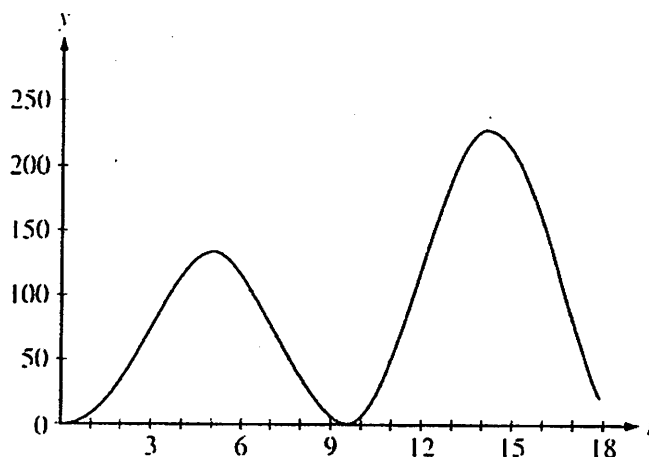
1. Traffic flow is defined as the rate at which cars pass through an intersection, measured in cars per minute. The traffic flow at a particular intersection is modeled by the function  $F$  defined by

$$F(t) = 82 + 4 \sin\left(\frac{t}{2}\right) \text{ for } 0 \leq t \leq 30,$$

where  $F(t)$  is measured in cars per minute and  $t$  is measured in minutes.

- (a) To the nearest whole number, how many cars pass through the intersection over the 30-minute period?
- (b) Is the traffic flow increasing or decreasing at  $t = 7$ ? Give a reason for your answer.
- (c) What is the average value of the traffic flow over the time interval  $10 \leq t \leq 15$ ? Indicate units of measure.
- (d) What is the average rate of change of the traffic flow over the time interval  $10 \leq t \leq 15$ ? Indicate units of measure.

2006 AP<sup>®</sup> CALCULUS AB FREE-RESPONSE QUESTIONS



2. At an intersection in Thomasville, Oregon, cars turn left at the rate  $L(t) = 60\sqrt{t} \sin^2\left(\frac{t}{3}\right)$  cars per hour over the time interval  $0 \leq t \leq 18$  hours. The graph of  $y = L(t)$  is shown above.
- To the nearest whole number, find the total number of cars turning left at the intersection over the time interval  $0 \leq t \leq 18$  hours.
  - Traffic engineers will consider turn restrictions when  $L(t) \geq 150$  cars per hour. Find all values of  $t$  for which  $L(t) \geq 150$  and compute the average value of  $L$  over this time interval. Indicate units of measure.
  - Traffic engineers will install a signal if there is any two-hour time interval during which the product of the total number of cars turning left and the total number of oncoming cars traveling straight through the intersection is greater than 200,000. In every two-hour time interval, 500 oncoming cars travel straight through the intersection. Does this intersection require a traffic signal? Explain the reasoning that leads to your conclusion.

AP<sup>®</sup> CALCULUS AB  
2005 SCORING GUIDELINES (Form B)

Question 2

A water tank at Camp Newton holds 1200 gallons of water at time  $t = 0$ . During the time interval  $0 \leq t \leq 18$  hours, water is pumped into the tank at the rate

$$W(t) = 95\sqrt{t} \sin^2\left(\frac{t}{6}\right) \text{ gallons per hour.}$$

During the same time interval, water is removed from the tank at the rate

$$R(t) = 275\sin^2\left(\frac{t}{3}\right) \text{ gallons per hour.}$$

- Is the amount of water in the tank increasing at time  $t = 15$ ? Why or why not?
- To the nearest whole number, how many gallons of water are in the tank at time  $t = 18$ ?
- At what time  $t$ , for  $0 \leq t \leq 18$ , is the amount of water in the tank at an absolute minimum? Show the work that leads to your conclusion.
- For  $t > 18$ , no water is pumped into the tank, but water continues to be removed at the rate  $R(t)$  until the tank becomes empty. Let  $k$  be the time at which the tank becomes empty. Write, but do not solve, an equation involving an integral expression that can be used to find the value of  $k$ .