

1990 AB5

Let  $f$  be the function defined by  $f(x) = \sin^2 x - \sin x$  for  $0 \leq x \leq \frac{3\pi}{2}$ .

- (a) Find the  $x$ -intercepts of the graph of  $f$ .
- (b) Find the intervals on which  $f$  is increasing.
- (c) Find the absolute maximum value and the absolute minimum value of  $f$ . Justify your answer.

1989 BC3

Consider the function  $f$  defined by  $f(x) = e^x \cos x$  with domain  $[0, 2\pi]$ .

- (a) Find the absolute maximum and minimum values of  $f(x)$ .
- (b) Find the intervals on which  $f$  is increasing.
- (c) Find the  $x$ -coordinate of each point of inflection of the graph of  $f$ .

1989 AB1

Let  $f$  be the function given by  $f(x) = x^3 - 7x + 6$ .

- (a) Find the zeros of  $f$ .
- (b) Write an equation of the line tangent to the graph of  $f$  at  $x = -1$ .
- (c) Find the number  $c$  that satisfies the conclusion of the Mean Value Theorem for  $f$  on the closed interval  $[1, 3]$ .

**1994 AB 1**

Let  $f$  be the function given by  $f(x) = 3x^4 + x^3 - 21x^2$ .

- (a) Write an equation of the line tangent to the graph of  $f$  at the point  $(2, -28)$ .
- (b) Find the absolute minimum value of  $f$ . Show the analysis that leads to your conclusion.
- (c) Find the  $x$ -coordinate of each point of inflection on the graph of  $f$ . Show the analysis that leads to your conclusion.

**1993 AB4/BC3**

Let  $f$  be the function defined by  $f(x) = \ln(2 + \sin x)$  for  $\pi \leq x \leq 2\pi$ .

- (a) Find the absolute maximum value and the absolute minimum value of  $f$ . Show the analysis that leads to your conclusion.
- (b) Find the  $x$ -coordinate of each inflection point on the graph of  $f$ . Justify your answer.

If  $f$  is continuous on  $[0, 3]$  and satisfies the following:

$x$	0	$0 < x < 1$	1	$1 < x < 2$	2	$2 < x < 3$	3
$f(x)$	0	+	2	+	0	-	-2
$f'(x)$	3	+	0	-	DNE	-	-3
$f''(x)$	0	-	-1	-	DNE	-	0

- a) Find the absolute extrema of  $f$  and where they occur. Justify your response.
- b) Find any points of inflection. Justify your response.

